Check-in

Review: Predictive Parsing

Assume an LL(1) parser with...

this selector table:

	()	{	}
S	(S))	{	}

this syntax stack:

and this (lookahead token:

S
)
eof

Draw the configuration of the parser after it processes the tokens ()



Projects

- P2 (nominally) due Wednesday
- P3 out Friday

Trials

• Trial 1 due tonight



Labs

 Based on the confusion about abstract classes, I've decided to shift the labs a bit University of Kansas | Drew Davidson

CORPEER CONSTRUCTION

FIRST Sets

Last Time Review – Predictive Parsing

Intro to Parsing

Complexity

A New Type of Language - LL(k)

- Intro
- LL(1) parsing

You Should Know

- What parsing is
- What LL(1) languages are
- How an LL(1) parser operates

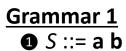


Parsing

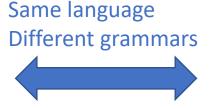
Where we Left Off

Review – Predictive Parsing

The language might be LL(1) ... even when the grammar is not!



2 | a c



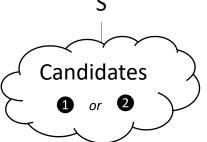
Grammar 2

1 *S* ::= **a** *X*

2 *X* ::= **b**

3 *X* ::= **c**

Predicted Parse Tree Input String





S Lookahead Candidates Candidates

Today's Outline Preview - FIRST Sets

Transforming Grammars

• Fixing LL(1) "near misses"

Building LL(1) Parsers

- What the selector table needs
- FIRST Sets



Parsing

LL(1) Grammar Limitations

Transforming Grammars – Fixing LL(1) Near Misses

Given a language, we can't always find an LL(1) grammar even if one exists

 Best we can do: simple transformations that remove "obvious" disqualifiers



Checking if a Grammar is LL(1)

Transforming Grammars – Fixing LL(1) Near Misses

If either of the following hold, the grammar is <u>not</u> LL(1):

- The grammar is left-recursive
- The grammar isn't left-factored



We can transform *some* grammars while preserving the recognized language

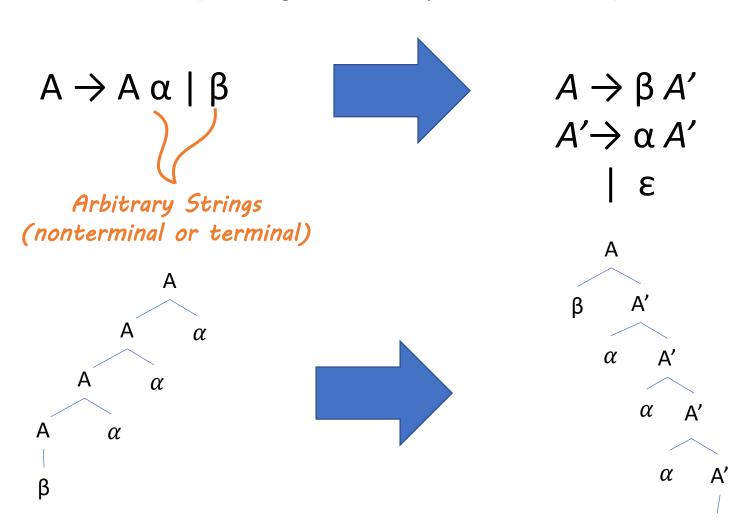
(Immediate) Left Recursion Transforming Grammars – Fixing LL(1) Near Misses

- Recall, a grammar such that $X \stackrel{+}{\Rightarrow} X \alpha$ is left recursive
- A grammar is immediately left recursive if this can happen in one step:

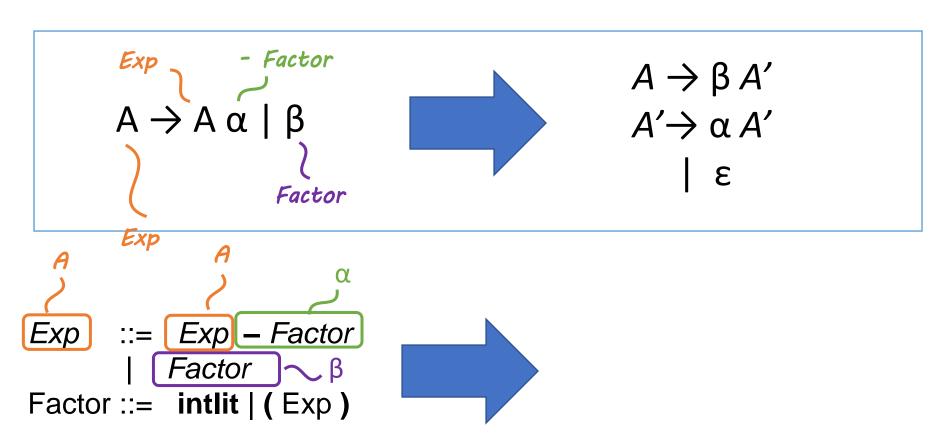
$$A \rightarrow A \alpha \mid \beta$$

(Predictive) Parsing - LL(1) Transformations

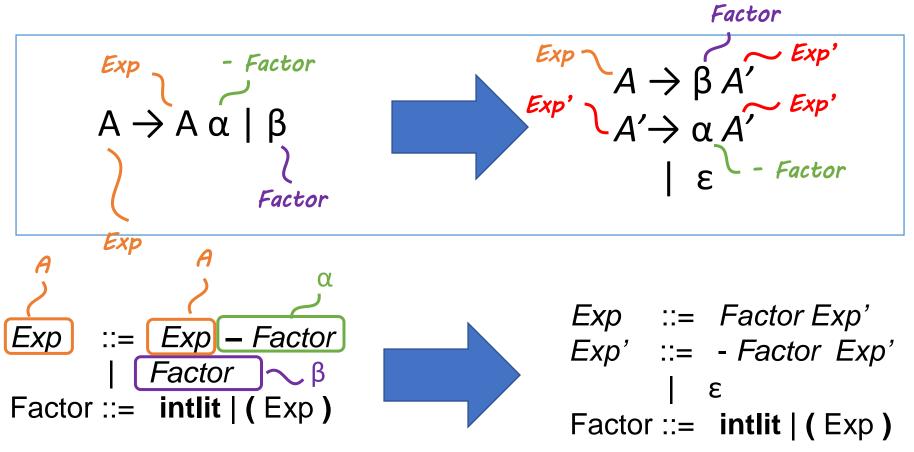
(for a single immediately left-recursive rule)



(Predictive) Parsing - LL(1) Transformations



(Predictive) Parsing - LL(1) Transformations



(Predictive) Parsing - LL(1) Transformations

(general rule)

Given Productions

$$A := \alpha_1$$

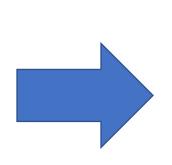
$$\mid \alpha_2$$

$$\mid \alpha_n$$

$$\mid A \beta_1$$

$$\mid A \beta_2$$

$$\mid A \beta_m$$



$$A ::= \alpha_1 A'$$

$$| \alpha_2 A'$$

$$| \alpha_n A'$$

$$A' ::= \beta_1 A'$$

$$| \beta_2 A'$$

$$| \beta_m A'$$

Convert to

Left Factoring Grammar (Predictive) Parsing - LL(1) Transformations

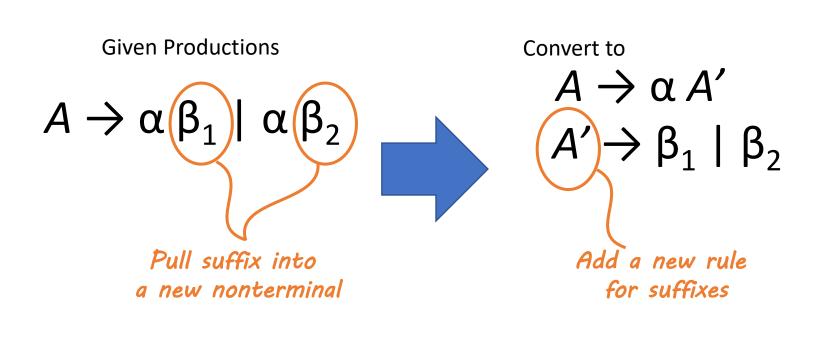
 If a nonterminal has (at least) two productions whose RHS has a common prefix, the grammar is not left factored

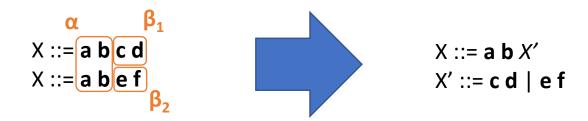
(and **not** an LL(1) grammar)

Question: What makes this grammar not left-factored?

Left Factoring: Simple Rule

(Predictive) Parsing - LL(1) Transformations





Attempt LL(1) Conversion

(Predictive) Parsing - LL(1) Transformations

Remove immediate left-recursion

Left-factored

$$A \rightarrow A \alpha \mid \beta$$

becomes

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A'$$

$$\mid \epsilon$$

Attempt LL(1) Conversion

(Predictive) Parsing - LL(1) Transformations

Remove immediate left-recursion

Left-factored

$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2$$
 becomes

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 \mid \beta_2$$

Attempt LL(1) Conversion

(Predictive) Parsing - LL(1) Transformations

Remove immediate left-recursion

$$A \rightarrow \alpha \; \beta_1 \; | \; \alpha \; \beta_2 \; ^{\text{becomes}}$$

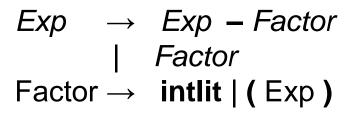
$$A \rightarrow \alpha A'$$

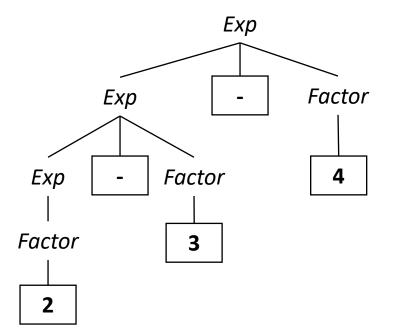
$$A' \rightarrow \beta_1 \mid \beta_2$$

Current Status (Predictive) Parsing - LL(1) Transformations

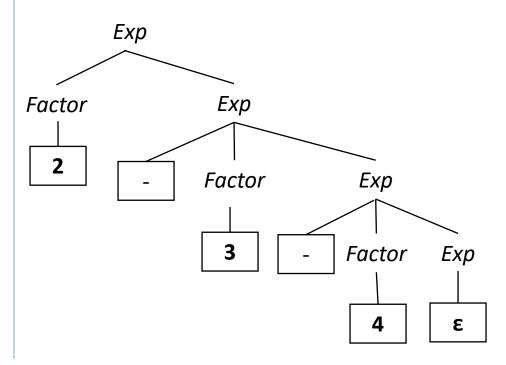
- We've removed 2 disqualifiers from LL(1)
 - Left-recursive grammar
 - Not Left-Factored grammar

Let's Check on the Parse Tree LL(1) Grammar Transformations



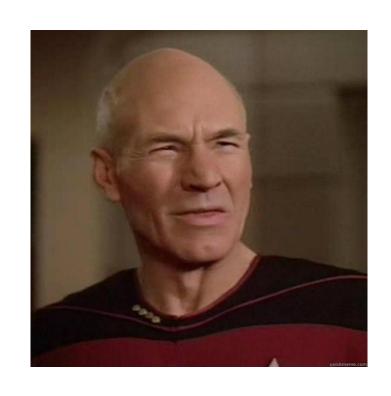


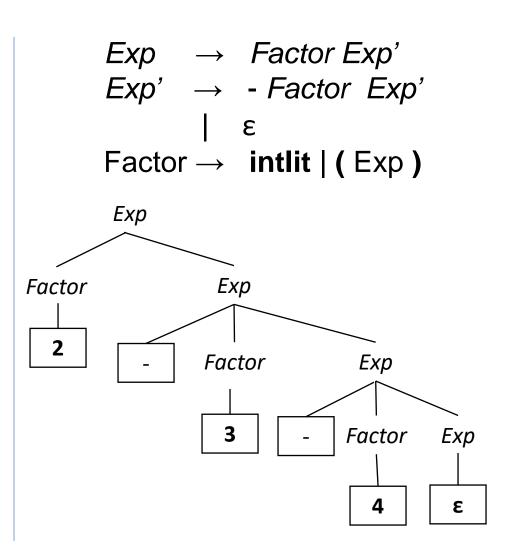
```
Exp \rightarrow Factor Exp'
Exp' \rightarrow -Factor Exp'
\mid \epsilon
Factor \rightarrow intlit \mid (Exp)
```



Let's Check on the Parse Tree

LL(1) Grammar Transformations





Nevermind, We'll Fix Parse Trees Later LL(1) Grammar Transformations

Today's Outline Lecture 9 - FIRST sets

Transforming Grammars



• Fixing LL(1) "near misses"

Building LL(1) Parsers

- Understanding LL(1) Selector Tables
- FIRST Sets



Parsing

Recall the LL(1) Parser's Operation Building LL(1) Selector Table

LL(1)

- Processes Left-to-right
- Leftmost derivation
- 1 token of lookahead

Predictive Parser: "guess & check"

- Starts at the root, guesses how to unfold a nonterminal (derivation step)
- Checks that terminals match prediction

Recall the LL(1) Parser's Operation Building LL(1) Selector Table

Example LL(1) Grammar:

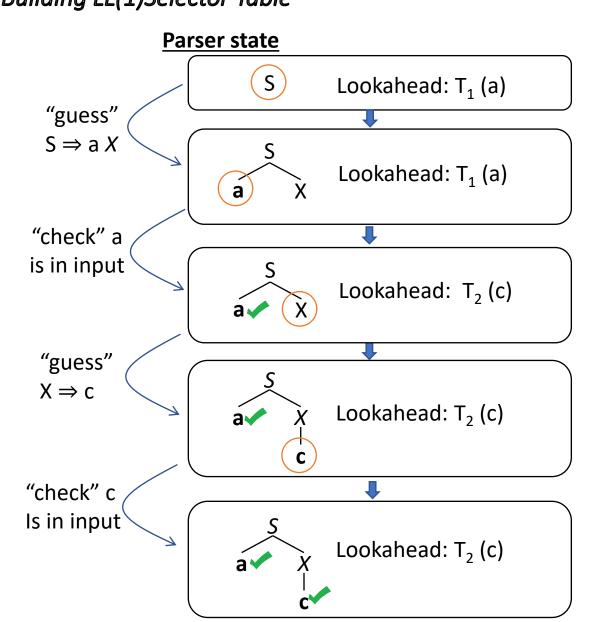
S ::= **a** *X*

X ::= **b** a | **c**

Example Input:

 $\begin{array}{ccc} \mathbf{a} & \mathbf{c} \\ \uparrow & \uparrow \\ \mathsf{T}_1 & \mathsf{T}_2 \end{array}$

In practice,
table-driven parser
uses a stack to
match this tree



How does the Parser Guess? Building Parser Tables

The intuition is a bit tricky

We need to get into the mindset of the parser



Pretend your consciousness has been transported inside an LL(1) parser

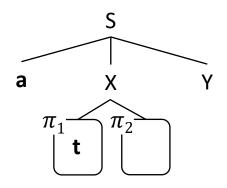
Building Parser Tables

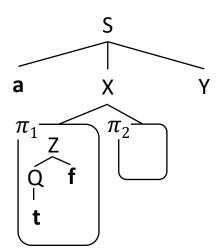
You need to unfold a nonterminal *X* with lookahead token **t**

Assume there's an X production $X := \pi_1 \pi_2$ (where π_1 and π_2 are some kind of symbol)

How do we know to guess this production?

Case 1: π_1 subtree may start with **t**





Parse in Progress

S

Lookahead: T₂ (t)

Grammar Fragment

 $\mathsf{X} ::= \pi_1 \; \pi_2$

Building Parser Tables

You need to unfold a nonterminal *X* with lookahead token **t**

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How do we know to guess this production?

Parse in Progress S

Lookahead: T₂ (t)

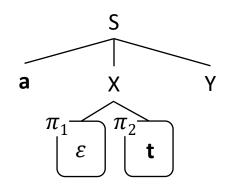
Grammar Fragment

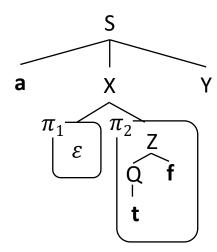
 $\mathsf{X} ::= \pi_1 \; \pi_2$

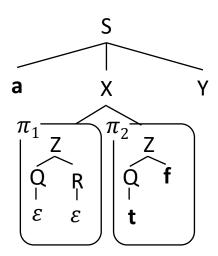
•••

Case 1: π_1 subtree may start with **t**

Case 2: π_1 subtree may be empty and π_2 starts with **t**







Building Parser Tables

You need to unfold a nonterminal *X* with lookahead token **t**

Assume there's an X production $X := \pi_1 \pi_2$ (where π_1 and π_2 are some kind of symbol)

How do we know to guess this production?

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Parse in Progress

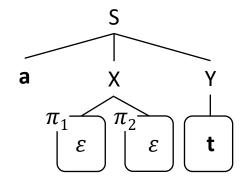
S

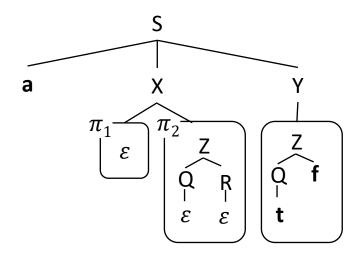
Lookahead: T₂ (t)

Grammar Fragment

 $X ::= \pi_1 \ \pi_2$

Case 3: both π_1 and π_2 may be empty and the sibling may start with ${\bf t}$





Building Parser Tables

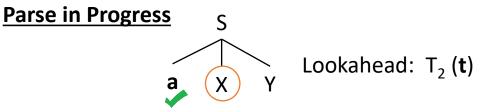
You need to unfold a nonterminal *X* with lookahead token **t**

Assume there's an X production $X := \pi_1 \pi_2$ (where π_1 and π_2 are some kind of symbol)

How do we know to guess this production?

Case 1: π_1 subtree may start with **t**

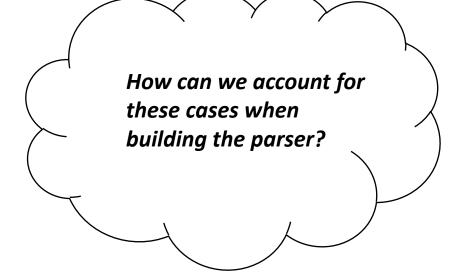
Case 2: π_1 subtree may be empty and π_2 starts with **t**



Grammar Fragment

 $X ::= \pi_1 \pi_2$

Case 3: both π_1 and π_2 may be empty and the sibling may start with ${\bf t}$



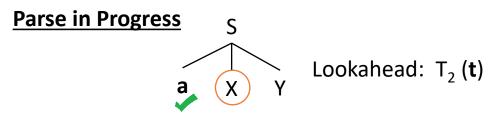
Building Parser Tables

You need to unfold a nonterminal *X* with lookahead token **t**

Assume there's an X production $X := \pi_1 \pi_2$ (where π_1 and π_2 are some kind of symbol)

How do we know to guess this production?





Grammar Fragment

 $\mathbf{X} ::= \pi_1 \ \pi_2$ Case 3: both π_1 and π_2 may be empty and the sibling may start with \mathbf{t} FOLLOW Sets

Two sets are sufficient to capture these cases and to build the selector table

Today's Outline Lecture 9 - FIRST sets

Transforming Grammars

• Fixing LL(1) "near misses"

Building LL(1) Parsers

- Reverse-Engineering Selector Tables
- FIRST Sets



Parsing

An Informal Definition

Building LL(1) Selector Table: FIRST sets, single symbol

FIRST(α) = The set of terminals that begin strings derivable from α , and also, if α can derive ϵ , then ϵ is in FIRST(X).

A Formal Definition

Building LL(1) Selector Table: FIRST sets, single symbol

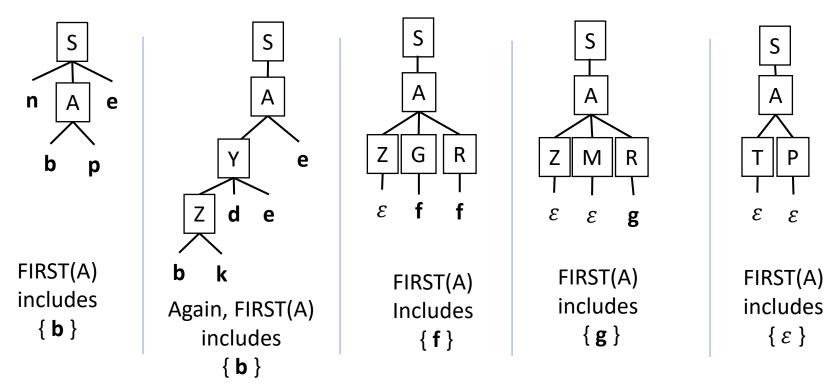
FIRST(α) = The set of terminals that begin strings derivable from α , and also, if α can derive ϵ , then ϵ is in FIRST(X).

Formally, FIRST(
$$\alpha$$
) =
$$\left\{ \widehat{\alpha} \mid \left(\widehat{\alpha} \in \Sigma \land \alpha \stackrel{*}{\Rightarrow} \widehat{\alpha} \beta \right) \lor \left(\widehat{\alpha} = \varepsilon \land \alpha \stackrel{*}{\Rightarrow} \varepsilon \right) \right\}$$

A Parse Tree Perspective Building LL(1) Selector Table: FIRST sets, single symbol

 $FIRST(\alpha)$ = The set of terminals that begin strings derivable from α , and also, if α can derive ϵ , then ϵ is in FIRST(X).

What does the parse tree say about FIRST(A)?



If these were the only possible parse trees, then FIRST(A) = { **b**, f, **g**, ε }

A Parse Tree Perspective Building LL(1) Selector Table: FIRST sets, single symbol

 $FIRST(\alpha)$ = The set of terminals that begin strings derivable from α , and also, if α can derive ϵ , then ϵ is in FIRST(X).

This isn't how you build FIRST sets

- Looking at parse trees is illustrative for concepts only
- We need to derive FIRST sets directly from the grammar

Building FIRST Sets: Methodology Building Parser Tables

First sets exist for any arbitrary string of symbols α

- Defined in terms of FIRST sets for a single symbol
 - FIRST of an alphabet terminal
 - FIRST for ε
 - FIRST for a nonterminal
- Use single-symbol FIRST to construct symbol-string FIRSTS

Rules for Single Symbols Building Parser Tables

FIRST(X) = The set of terminals that begin strings derivable from X, and also, if X can derive ε , then ε is in FIRST(X).

Building FIRST for terminals

$$FIRST(t) = \{ t \} for t in \Sigma$$

$$FIRST(\varepsilon) = \{ \varepsilon \}$$



Building FIRST(X) for nonterminal X

For each $X ::= \alpha_1 \alpha_2 ... \alpha_n$

 C_1 : add FIRST(α_1) - ε

C₂: If ε could "prefix" FIRST(α_k), add FIRST(α_k)- ε

 C_3 : If ε is in every FIRST set $\alpha_1 \dots \alpha_n$, add ε

Rules for Single Symbols Building LL(1) Parsers

Building FIRST(X) for nonterminal X

For each $X ::= \alpha_1 \alpha_2 ... \alpha_n$

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Rules for Single Symbols Building LL(1) Parsers

Building FIRST(X) for nonterminal X

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 C_3 : If ε is in every FIRST set $\alpha_1 \dots \alpha_n$, add ε

Say there's a production

$$X ::= YZRT$$

and we know

FIRST(
$$Y$$
) = { ε , \mathbf{a} }

$$FIRST(Z) = \{ \varepsilon, \mathbf{b}, \mathbf{m} \}$$

$$FIRST(R) = \{ c \}$$

$$FIRST(T) = \{ d \}$$

By C₂ clause FIRST(X) includes **b**, **m** and **c**

b,m because FIRST of every symbol before the 2^{nd} includes ε)

Z in this case

c because FIRST of every symbol before the 3^{rd} includes ε)

R in this case

FIRST(X) does not add \mathbf{d} in this clause because not every FIRST set before the T includes ε

Building FIRST Sets for Symbol Strings Building LL(1) Parsers

Building FIRST(α)

Let α be composed of symbols $\alpha_1 \alpha_2 \dots \alpha_n$

 C_1 : add FIRST(α_1) - ε

C₂: If $\alpha_1 \dots \alpha_{k-1}$ is nullable, add FIRST(α_k)- ε

 C_3 : If $\alpha_1 \dots \alpha_n$ is nullable, add ε

Base Cases:

 α_i is is a terminal **t**. Add **t**

 α_i is is a nonterminal X. Add every leaf symbol that could begin an X subtree (this gets a bit complicated due to dependencies)

Summary: Explored the LL(1) Mindset FIRST Sets

LL(1) "Parseability" Qualification

 Knowing the leftmost terminal of a parse (sub)tree is enough to pick the next derivation step

Elusive Conditions

- Two different rules could start with the same terminal (not left factored)
- The same rule(s) could be applied repeatedly (left recursive)

Began choosing matching productions to input

What terminal could the production be the start of (FIRST)?